

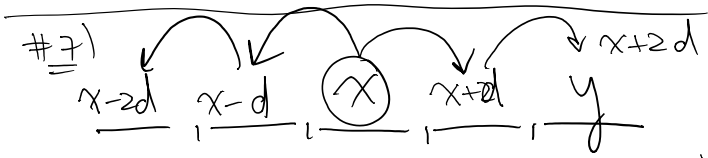
HW 2.1

March 8, 2015 2:45 PM

HW #9)

$$\begin{aligned}
 T_n &= 3n - 1 \\
 T_1 &= 2 \\
 T_2 &= 5 \\
 T_3 &= 8 \\
 T_4 &= 11
 \end{aligned}$$

$$\begin{aligned}
 S_n &= \frac{n}{2} (2(a) + (n-1)d) \\
 &= \frac{n}{2} (4 + (n-1)3) \\
 &= \frac{n}{2} [4 + 3n - 3] \\
 &= \frac{n}{2} [1 + 3n] \quad \text{☺}
 \end{aligned}$$



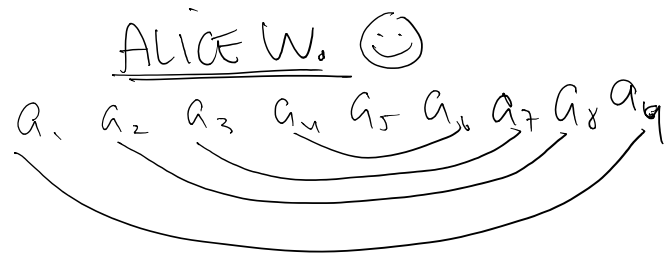
$$\begin{aligned}
 x + 2d &= y \\
 2d &= y - x \\
 t_1 &= x - (2d) \\
 &= x - (y - x) \\
 &= 2x - y
 \end{aligned}$$

#5)

$$\begin{aligned}
 a_5 + a_7 &= -17 & a_4 + a_6 &= 1
 \end{aligned}$$

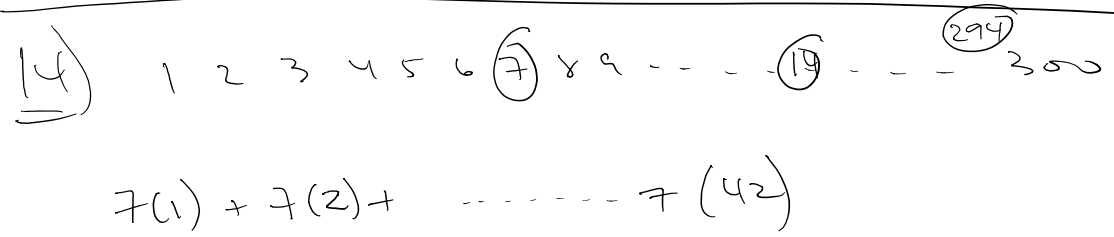
#3)

$$\begin{aligned}
 2a + 10d &= -17 \\
 2a + 8d &= 1 & 2a + 8(d) &= 1 \\
 2d &= -18 & 2a &= 1 + 72 \\
 d &= -9 & a &= \frac{73}{2}
 \end{aligned}$$



$$\begin{aligned}
 S_n &= \frac{9}{2} (a_1 + a_6) \\
 &= \frac{9}{2} (1) \\
 &= \frac{9}{2} //
 \end{aligned}$$

$$\begin{aligned}
 S_9 &= \frac{9}{2} [2(\frac{73}{2}) + (8)(-9)]
 \end{aligned}$$



$n = 42$
$d = 7$
$a = 7$

16)

$a, a+d, a+2d, a+3d, a+4d, a+5d, a+6d, a+7d, \dots$

must include last term

① $a + a+2d + a+4d + a+6d + a+8d + \dots + a+6kd = 320$
 # of terms = $3k+1$

② $a + a+3d + a+6d + a+9d + \dots + a+6kd = 224$
 # of terms = $2k+1$

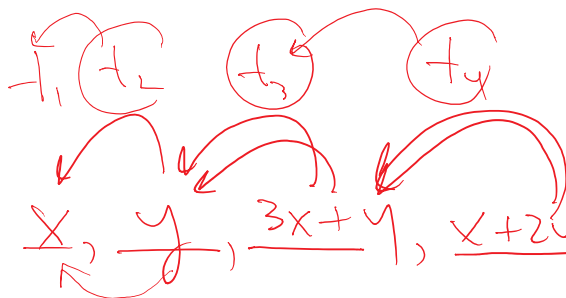
2 step How many terms are in each seq.

$(3k+1) \left(\frac{\text{PAIR}}{2} \right) = 320$

$(2k+1) \left(\frac{\text{PAIR}}{2} \right) = 224$

DIVIDE THEM THEN SOLVE FOR "k"

③ AFTER YOU FIND "k", FIND THE VALUE OF EACH "PAIR"



10)

$x, y, 3x+y, x+2y+2$

" $y-x$ " = ??

① $y-x = 3x+y-y$

② $x+2y+2 - 3x - y = 3x+y-y$

$y-x = 3x$
 $y = 4x$

$y+2 = 5x$
 $4+2 = 5x$

$$y = 4x$$

$$y = 8$$

$$4x + 2 = 5x$$

$$2 = x$$

$$\cancel{y} - x = x + \cancel{2y} + 2 - 3x - \cancel{y}$$

$$2x = x + 2$$

$$x = 2$$

a) $t_{16} = 58$

b) $t_9 = 72$

c) $t_8 = -9.2$

d) $t_8 = \frac{65}{6}$

e) $t_6 = 21$

f) $t_6 = 32$

October-21-15

1:00 PM

Ch 2.1 By Alice Wang

2)	# of terms	SUM
a)	52	-8497.5
4. b) $a + (n-1)d$	$9 + (63-1)12$	
c) $\frac{a+t_n}{2}$	$\frac{9+72}{2}$	165
d) $\frac{a+t_n}{2}$	$\frac{8+40}{2}$	-488
e)	31	2697

f) $x = 4$ or 2 , multiple answers?

3. $\frac{3+5+9+12+21}{5} = \underline{\underline{d) 10}}$

5. $a+d=2a$ $2a+d=b$ $b+d=a-b-b$
 $d=a$ $d=b-2a$ $d=a-2b-b$

$$b=3a$$

$$a = a - 2(3a) - b$$

$$a = -1$$

$$b = -3$$

$$d = -1$$

$$t_{100} = -1 + (100-1)(1)$$

$$= -1 + (-9a)$$

$$\boxed{t_{100} = a - 100}$$

6. (i) $T_n = 2n - 3$

ii) is geometric

7. $\underbrace{a, -, x, -, y}$

$$a + y = 2x$$

$$a = 2x - y$$

(i) $2x - y$

8. $-16, -14.75, -13.5$

$$\underbrace{-16, -14.75}_{+1.25}, \underbrace{-14.75, -13.5}_{+1.25}$$

$$t_n = -16 + (n-1)1.25$$

$$t_n = 1.25n - 17.25$$

$$1.25 \times 14 > 17.25$$

$$n = 14, t_n = 0.25$$

9. $T_1 = 2, T_2 = 5, T_3 = 8$

(ii) $\frac{n(3n+1)}{2}$

10. $x + d = y$
 $d = y - x$

$$y + d = 3x + y$$

$$y + y - x = 3x + y$$

$$y = 4x$$

$$3x + y + d = x + 2y + 2$$

$$3x + 4x + 4x - x = x + 8x + 2$$

$$10x = 9x + 2$$

$$x = 2$$

$$y = 8$$

(e) 6

11. $x, x+y, x+2y, x+3y$

$$x + x + 2y = 30$$

$$x + y = 15$$

$$x = 15 - y$$

$$4x + 6y = 82$$

$$2x + 3y = 41$$

$$2(15 - y) + 3y = 41$$

$$30 - 2y + 3y = 41$$

$$y = 11, x = 4$$

$$x + y = 15$$

$$x + 3y = 37$$

4th term
is greater
by 22

12. $a, 2, a+2, 2(a+2),$

$$8(a+2) = 56$$

$$a + 2 = 7$$

(a = e) 5

13. $309 = -300 + (n-1)3$

$$309 = -300 + 3n - 3$$

$$612 = 3n$$

$$n = 204$$

$$S_n = \frac{204}{2}(-300 + 319)$$

(S_n = d) 918

$$14. \quad 7, 14, 21, 28 \dots 294$$

$$\underbrace{\quad}_{+7}$$

$$S_n = \frac{42}{2}(7+294)$$

$$294 = 7 + (n-1)7$$

$$S_n = 21(301)$$

$$294 = 7n$$

$$n = 42$$

$$\boxed{S_n = 6321}$$

$$15. \quad a_4 + a_6 = 1$$

$$1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9$$



$$S_n = \frac{a}{2}(1)$$

$$\boxed{S_n = 4.5}$$

$$17. \quad A: a, a+d, a+2d$$

$$ax = 11+d \quad (11+d)x = 2a+2d$$

$$G: a, 11+d, 2a+2d$$

$$d = ax - 11 \quad 11x + dx = 2a + 2d$$

$$11x + (ax - 11)x = 2a + 2(ax - 11)$$

$$11x + ax^2 - 11x = 2a + 18x - 22$$

$$ax^2 - 18x - 7 = 0$$

$$(3x+1)(3x-7) = 0$$

$$x = -\frac{1}{3} \quad x = \frac{7}{3}$$

$$a(-\frac{1}{3}) = 11+d$$

$$-3 = 11+d$$

$$d = -14$$

$$2a + 2d = 1$$

$$\boxed{= a) 1}$$